# L-Shaped RST Routing

- Perform L-RST using node *b* as the root
	- **Service Service** First step: build a separable MST
	- $\mathbb{R}^3$ Prim with  $w(i,j) = (D(i,j), -|y(i) - y(j)|, -\max\{x(i), x(j)\})$





### First Iteration

We initially set our separable MST  $T = \{b\}$ . T contains three nearest neighbors:  $a, d$ , and f. These nodes can connect to T via the following edges (sorted based on their weights):

- $(b, d) = (4, -3, -4)$
- $(b, f) = (4, -1, -7)$
- $(b, a) = (4, -1, -4)$

Thus, we add  $(b, d)$  to T based on this lexicographical order.





#### Separable MST Construction





**Physical Design L-RST Algorithm (3/16)**

#### Separable MST Construction (cont)



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## Constructing a Rooted Tree

- $\blacksquare$  Node *b* is the root node
	- **Service Service** Based on the separable MST (initial wirelength  $= 32$ )
	- $\mathbb{R}^3$  Bottom-up traversal is performed on this tree during L-RST routing





**Physical Design L-RST Algorithm (5/16)**

#### Partial L-RST for Node C

- $\bullet$   $\Phi_l(c)$ :  $(c, d)$  is fixed to lower-L. Figure (a) shows  $\Phi_l(c)$ . We assign lower-L to  $(c, a)$  in order to maximize the overlap in  $T_c^S$ . Thus,  $Z(\Phi_l(c))=1.$
- $\bullet$   $\Phi_u(c)$ :  $(c, d)$  is fixed to upper-L. Figure (b) shows  $\Phi_u(c)$ . The orientation of  $(c, a)$  is irrelevant because no overlap occurs in  $T_c^S$ . Thus,  $Z(\Phi_u(c)) = 0$ .



#### Partial L-RST for Node E

- $\bullet$   $\Phi_l(e)$ :  $(e, f)$  is fixed to lower-L. Figure (a) shows  $\Phi_l(e)$ . The orientation of  $(e, i)$  is irrelevant because no overlap occurs in  $T_e^S$ . Thus,  $Z(\Phi_l(e)) = 0$ .
- $\bullet$   $\Phi_u(e)$ :  $(e, f)$  is fixed to upper-L. Figure (b) shows  $\Phi_u(e)$ . We assign lower-L to  $(e, i)$  in order to maximize the overlap in  $T_e^S$ . Thus,  $Z(\Phi_u(e)) = 1$ .



#### Partial L-RST for Node G

- $\bullet$   $\Phi_l(g)$ :  $(g, f)$  is fixed to lower-L. Figure (a) shows  $\Phi_l(g)$ . The orientation of  $(g, h)$  is irrelevant because no overlap occurs in  $T_q^S$ . Thus,  $Z(\Phi_l(g)) = 0$ .
- $\bullet$   $\Phi_u(g)$ :  $(g, f)$  is fixed to upper-L. Figure (b) shows  $\Phi_u(g)$ . We assign upper-L to  $(g, h)$  in order to maximize the overlap in  $T_q^S$ . Thus,  $Z(\Phi_u(g)) = 1$ .



#### Partial L-RST for Node D

 $\bullet$   $\Phi_l(d)$ :  $(d, b)$  is fixed to lower-L. Figure (a) shows  $\Phi_l(d)$ . There is no overlap in  $T_d^S$ , but we choose lower-L for  $(d, c)$  because  $Z(\Phi_l(c)) > Z(\Phi_u(c))$  from Part (a). Thus,

$$
Z(\Phi_l(d)) = Z(T_d^S) + \max\{Z(\Phi_l(c)), Z(\Phi_u(c))\}
$$
  
= 0 + \max\{1, 0\} = 1



#### Partial L-RST for Node D (cont)

 $\bullet$   $\Phi_u(d)$ :  $(d, b)$  is fixed to upper-L. Figure (b) shows  $\Phi_u(d)$ . There is no overlap in  $T_d^S$ , but we choose lower-L for  $(d, c)$  because  $Z(\Phi_l(c)) > Z(\Phi_u(c))$  from Part (a). Thus,

$$
Z(\Phi_u(d)) = Z(T_d^S) + \max\{Z(\Phi_l(c)), Z(\Phi_u(c))\}
$$
  
= 0 + \max\{1, 0\} = 1



#### Partial L-RST for Node F

 $\bullet$   $\Phi_l(f)$ :  $(f, b)$  is fixed to lower-L. Since f has two children e and g, we consider the following 4 cases:

$$
Z(\Phi_l(f)) = Z(T_f^S) + Z(\Phi_l(e)) + Z(\Phi_l(g))
$$
  
\n
$$
= 1 + 0 + 0 = 1
$$
  
\n
$$
Z(\Phi_l(f)) = Z(T_f^S) + Z(\Phi_l(e)) + Z(\Phi_u(g))
$$
  
\n
$$
= 0 + 0 + 1 = 1
$$
  
\n
$$
Z(\Phi_l(f)) = Z(T_f^S) + Z(\Phi_u(e)) + Z(\Phi_l(g))
$$
  
\n
$$
= 1 + 1 + 0 = 2 \text{ best case}
$$
  
\n
$$
Z(\Phi_l(f)) = Z(T_f^S) + Z(\Phi_u(e)) + Z(\Phi_u(g))
$$
  
\n
$$
= 0 + 1 + 1 = 2
$$





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#### Partial L-RST for Node F (cont)

 $\bullet$   $\Phi_u(f)$ :  $(f, b)$  is fixed to upper-L. We again consider the following 4 cases to compute the total amount of overlap in  $\Phi_u(f)$ :

$$
Z(\Phi_u(f)) = Z(T_f^S) + Z(\Phi_l(e)) + Z(\Phi_l(g))
$$
  
\n
$$
= 1 + 0 + 0 = 1
$$
  
\n
$$
Z(\Phi_u(f)) = Z(T_f^S) + Z(\Phi_l(e)) + Z(\Phi_u(g))
$$
  
\n
$$
= 1 + 0 + 1 = 2 \text{ best case}
$$
  
\n
$$
Z(\Phi_u(f)) = Z(T_f^S) + Z(\Phi_u(e)) + Z(\Phi_l(g))
$$
  
\n
$$
= 0 + 1 + 0 = 1
$$
  
\n
$$
Z(\Phi_u(f)) = Z(T_f^S) + Z(\Phi_u(e)) + Z(\Phi_u(g))
$$
  
\n
$$
= 0 + 1 + 1 = 2
$$





#### Processing the Root Node

b has two children d and f. Since b is the root node, we examine the following 4 cases and choose the best solution (no additional partial L-RST construction is necessary):

$$
Z(\Phi(b)) = Z(T_b^S) + Z(\Phi_l(d)) + Z(\Phi_l(f))
$$
  
= 0 + 1 + 2 = 3  

$$
Z(\Phi(b)) = Z(T_b^S) + Z(\Phi_l(d)) + Z(\Phi_u(f))
$$
  
= 0 + 1 + 2 = 3  

$$
Z(\Phi(b)) = Z(T_b^S) + Z(\Phi_u(d)) + Z(\Phi_l(f))
$$
  
= 0 + 1 + 2 = 3  

$$
Z(\Phi(b)) = Z(T_b^S) + Z(\Phi_u(d)) + Z(\Phi_u(f))
$$
  
= 1 + 1 + 2 = 4 **best case**





Top-down Traversal

**IF** In order to obtain the final tree



# Final Tree

- **Nirelength reduction** 
	- $\mathcal{L}_{\mathcal{A}}$ Initial wirelength – total overlap =  $32 - 4 = 28$



### Stable Under Rerouting

- Steiner points are marked X
	- **Service Service** Wirelength does not reduce after rerouting





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**Physical Design L-RST Algorithm (16/16)**